

**Problem 6** (15 points)

An instructor gives a painted piece of metal to 2 students and asks: "This is one of the metals listed in the table of densities. What metal do you think it is?"

The students measure the object and find that the mass is  $139.2 \pm 0.1 \text{ g}$  and the volume is  $16.0 \pm 0.5 \text{ cm}^3$ .

Student 1 says: "It must be nickel."

Student 2 says: "Don't forget the uncertainty. It might be silver."

Table of densities

Substance	Density
Tungsten	19 g/cm <sup>3</sup>
Lead	11.3 g/cm <sup>3</sup>
Silver	10.5 g/cm <sup>3</sup>
Copper	8.9 g/cm <sup>3</sup>
Nickel	8.7 g/cm <sup>3</sup>
Brass	8.5 g/cm <sup>3</sup>
Iron	7.9 g/cm <sup>3</sup>

A. What would you conclude from the data?

I would conclude that with such a large uncertainty in the volume, it could be either Brass, Nickel, or Copper. They all fit within the range of uncertainty.

Dr. Saul: Good solution, but should also mention that is the sample is probably not silver since the density for silver lies outside the range of possible densities. This is a composite solution from 2 students.

Handwritten student work showing mass and volume ranges, density calculations, and a conclusion.

Mass:  $139.1 \text{ g}$  to  $139.3 \text{ g}$  (range  $\pm 0.1 \text{ g}$ )

Volume:  $15.5 \text{ cm}^3$  to  $16.5 \text{ cm}^3$  (range  $\pm 0.5 \text{ cm}^3$ )

Possibilities of density:

- Lowest:  $\frac{139.1 \text{ g}}{16.5 \text{ cm}^3} \approx 8.43 \frac{\text{g}}{\text{cm}^3}$
- Highest:  $\frac{139.3 \text{ g}}{15.5 \text{ cm}^3} \approx 8.99 \frac{\text{g}}{\text{cm}^3}$

It could be Brass, Nickel, or Copper.

B. Do you agree with student 1, student 2, or neither? Explain your reasoning.

Student Solution: (Dr. Saul: hits all the key points)

disagree with student 1 b/c it doesn't have to be nickel. (like in part a, it could be Brass, Nickel, or copper.)

I disagree with Student 2 b/c it cannot be silver even when remembering the uncertainty.

But I do think it is imperative to remember the uncertainty so I do agree with that part of the statement. 😊