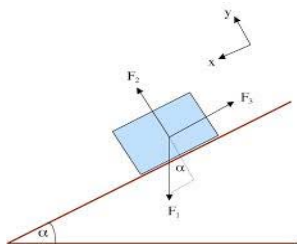
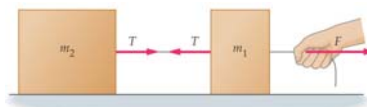


Free body diagram examples



Example #1



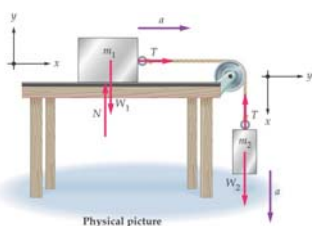
Physical picture

If $F=100\text{N}$, $m_1=2\text{kg}$ and $m_2=3\text{kg}$, (a) what is the tension on the string that connecting the two boxes? (b) what is the acceleration of m_1 ?

$$\begin{aligned}
 F - T &= m_1 a & \Rightarrow & \quad 100 - T = 2a & \Rightarrow & \quad 100 = 5a & \Rightarrow & \quad a = 20 \text{ m/s}^2 \\
 T &= m_2 a & \Rightarrow & \quad T = 3a & \Rightarrow & \quad T = 60 \text{ N}
 \end{aligned}$$

Example #2

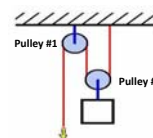
Assume $m_1=20\text{ kg}$, $m_2=10\text{ kg}$, and there is no friction. Find the acceleration and tension.



Physical picture

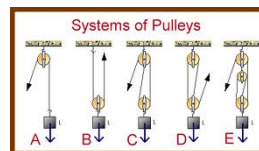
$$\begin{aligned}
 T &= m_1 a & \Rightarrow & \quad T = 20a & \Rightarrow & \quad 98 = 30a \\
 m_2 g - T &= m_2 a & \Rightarrow & \quad 98 - T = 10a & \Rightarrow & \quad 98 = 30a \\
 & & \Rightarrow & \quad a = 3.27 \frac{\text{m}}{\text{s}^2} & & \quad T = 65.3 \text{ N}
 \end{aligned}$$

Assume that the mass of the box is 100 kg, what is the force needed to lift the box?



Do a free body diagram on Pulley #2.

$$2T = mg \Rightarrow 2T = 980 \text{ N} \Rightarrow T = 490 \text{ N}$$



Find the tension on each string.

$$\begin{aligned}
 T_3 &= mg = 5.0 \times 9.8 = 49 \text{ N} \\
 T_2 \cos 50^\circ - T_1 \cos 40^\circ &= 0 \Rightarrow T_2 = 1.20 T_1 \\
 T_2 \sin 50^\circ + T_1 \sin 40^\circ &= T_3 = 49 \text{ N} \\
 \Rightarrow 1.20 T_1 \times 0.766 + T_1 \times 0.642 &= 49 \text{ N} \\
 \Rightarrow T_1 &= 31.4 \text{ N}, \quad T_2 = 37.7 \text{ N}
 \end{aligned}$$

A 5.0-kg block is placed on top of a 10-kg block. A horizontal force of 45 N is applied to the 10-kg block, and the 5.0 kg block is tied to the wall. The coefficient of kinetic friction between the moving surfaces is 0.20. Find tension of the rope and the acceleration of the 10-kg block.

